



Lecture 4: Backtracking and Cut



# Backtracking and Cut



**Review Backtracking**

**Cut**

**Cut uses**

**Problems with Cut**

# Backtracking

## Example

```

pair (X, Y) :-                ?- pair (X, Y) .
    boy (X), girl (Y) .      X=john, Y=griselda ;
boy (john) .                 X=john, Y=ermintrude ;
boy (marmaduke) .           X=john, Y=brunhilde ;
boy (bertram) .             X=marmaduke, Y=griselda ;
boy (charles) .             X=marmaduke, Y=ermintrude ;
girl (griselda) .          X=marmaduke, Y=brunhilde ;
girl (ermintrude) .        X=bertram, Y=griselda ;
girl (brunhilde) .         ...

```

12 solutions.

# Backtracking and Cut



Review Backtracking

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# The "Cut"

Cut (written "!") tells the system which previous choices need not to be considered again when it backtracks.

Advantages:

- ▶ The program will run faster. No time wasting on attempts to re-satisfy certain goals.
- ▶ The program will occupy less memory. Less backtracking points to be remembered.

# Example of Cut

- `sum_to` is a predicate to compute the summation from  $N$  to 1.
  1. `sum_to(1,1).`
  2. `sum_to(N, R):-`
  3.     `N1 is N-1,`
  4.     `sum_to(N1,R1),`
  5.     `R is N+R1.`
- The program will recursively call `sum_to` and each time  $N$  reduced by one until reaching **`sum_to(1, R)`**
- The problem is that, when prolog tries to match **`sum_to(1,R)`** both predicates in line 1 and 2 are a valid match. So the program will enter infinite loop after the first solution.

# Example of Cut

- Possible solution is to add line 3 to the program

1. `sum_to(1,1).`
2. `sum_to(N, R):-`
3. `N1 > 1, % or \+ (N1=<1)`
4. `N1 is N-1,`
5. `sum_to(N1,R1),`
6. `R is N+R1.`

(\+) is a built in predicate in prolog used as ( Not ) operation

- Even this solution will solve the problem, the prolog still backtrack to `sum_to(N, R)` as an alternative solution for `sum_to( 1, R)`.

# Example of Cut

- A perfect solution is to add “!” in line 1.

1. `sum_to(1,1):- !.`
2. `sum_to(N, R):-`
3.     `N1 is N-1,`
4.     `sum_to(N1,R1),`
5.     `R is N+R1.`

- Now, after prolog matches `sum_to( 1, R)` with the first alternative `sum_to(1,1)`. The Cut “!” will succeed and prevent the prolog to backtrack for other alternatives.



# Backtracking and Cut



9

Lecture 4: Backtracking and Cut

13-Apr-16

Review Backtracking

Cut

Common uses of Cut

Problems with Cut

# Common Uses of Cut

Three main cases:

1. To tell the system that it found the right rule for a particular goal. *Confirming the choice of a rule.*
2. To tell the system to fail a particular goal without trying for alternative solutions. *Cut-fail combination.*
3. To tell the system to terminate the generation of alternative solutions by backtracking. *Terminate a "generate-and-test."*

# Confirming the Choice of a Rule (use 1)

□ Exatly like the previous example

1. `sum_to(1,1):- !.`
2. `sum_to(N, R):-`
3.       `N1 is N-1,`
4.       `sum_to(N1,R1),`
5.       `R is N+R1.`

# Fail



`fail.`

- ▶ Built-in predicate.
- ▶ No arguments.
- ▶ Always fails as a goal and causes backtracking.

# The "Cut-fail" Combination (Use 2)

fail after cut:

- ▶ The normal backtracking behavior will be altered by the effect of cut.
- ▶ Quite useful combination in practice.

# The Fees discount

- Suppose there is a discount for 3<sup>rd</sup> grade students on the college fees this year. However, this discount is not applied on Foreign students.
- So if we have a foreign student  $x$ , the discount predicate should fail. We can write this as following

```
1. grade3_fees(X, Discount, Fees):- foreigner(X), fail.  
2. grade3_fees(X, Discount, Fees):- Fees is 200-Discout.
```

- The problem is: Even, 'fail' will cause line one to fail it will also force backtracking to the second line which will apply the discount for the foreign student.

# The Fees discount

- A good solution is to combine ‘!’ with fail to prevent the backtracking. This means that predicate in line one will fail (no discount for foreigners) , at the same time, prolog will not backtrack to other alternatives.

```
1. grade3_fees(X, Discount, Fees):- foreigner(X), !, fail.  
2. grade3_fees(X, Discount, Fees):- Fees is 200-Discount.
```

- Another readable solution for this is:

```
grade3_fees(X, Discount, Fees):- \+foreigner(X), Fees is 200-Discount.
```

# Terminating a "Generate-and-Test" (Use 3)



## "Generate-and-Test":

- ▶ One of the simplest AI search techniques.
- ▶ **Generate**: Generate all possible solutions to a problem.
- ▶ **Test**: Test each to see whether they are a solution.
- ▶ A possible solution is generated and then tested.
- ▶ If the test succeeds a solution is found.
- ▶ otherwise, backtrack to next possible solution.



# Example 1: Tic-Tac-Toe

Tic-Tac-Toe game: Get three in a row, column, or diagonal:

X		O
O	O	
X	X	X

X	X	O
O	X	
O	X	

O		O
X	O	
X	X	O

Representation:

1	2	3
4	5	6
7	8	9

# Tic-Tac-Toe

- We can represent the successful lines in the board as following:

```
line(b(X,Y,Z,_,_,_,_,_,_), X, Y, Z).  
line(b(_,_,_,X,Y,Z,_,_,_), X, Y, Z).  
line(b(_,_,_,_,_,_,X,Y,Z), X, Y, Z).  
line(b(X,_,_,Y,_,_,Z,_,_), X, Y, Z).  
line(b(_,X,_,_,Y,_,_,Z,_), X, Y, Z).  
line(b(_,_,X,_,_,Y,_,_,Z), X, Y, Z).  
line(b(X,_,_,_,Y,_,_,_,Z), X, Y, Z).  
line(b(_,_,X,_,Y,_,Z,_,_), X, Y, Z).
```

# Tic-Tac-Toe

- Consider the player  $o$  will have a threatening if player  $x$  completed two cells in a successful line, and the third is empty.

`threatening(e, x, x).`

`threatening(x, e, x).`

`threatening(x, x, e).`

- Threatening here means that player  $o$  have no choice other than filling the empty cell.

# Tic-Tac-Toe

- Now player **o** will provide our small program with the board status and want to make sure there is no threatening before his move.

```
forced_move(Board) :-  
    line(Board, X, Y, Z), %generate  
    threatening(X, Y, Z), %test  
    !.
```

# Tic-Tac-Toe



21

Lecture 4: Backtracking and Cut

13-Apr-16

- Here, a complete view for this part of the program:

```
line(b(X,Y,Z,_,_,_,_,_,_), X, Y, Z).  
line(b(_,_,_,X,Y,Z,_,_,_), X, Y, Z).  
line(b(_,_,_,_,_,_,X,Y,Z), X, Y, Z).  
line(b(X,_,_,Y,_,_,Z,_,_), X, Y, Z).  
line(b(_,X,_,_,Y,_,_,Z,_,_), X, Y, Z).  
line(b(_,_,X,_,_,Y,_,_,Z), X, Y, Z).  
line(b(X,_,_,_,Y,_,_,_,Z), X, Y, Z).  
line(b(_,_,X,_,Y,_,Z,_,_), X, Y, Z).
```

```
threatening(e, x, x).  
threatening(x, e, x).  
threatening(x, x, e).
```

```
forced_move(Board) :-  
line(Board, X, Y, Z), %generate  
threatening(X, Y, Z), %test  
!.
```

# Tic-Tac-Toe



22

Lecture 4: Backtracking and Cut

13-Apr-16

- If the player o provide the following goal:  
`forced_move(b(x,x,e,e,o,x,o,e,e))`.
- The program will return True and the **cut** will terminate the backtracking process because one threatening is enough for player o to know where he should play.

## Example 2: Divide two numbers.

- Simply this program generate an integer starting from 0 and test the condition line 5.

```
1. divide(N1, N2, Result) :-  
2.     is_integer(Result),  
3.     Product1 is Result * N2,  
4.     Product2 is (Result + 1) * N2,  
5.     Product1 =< N1, Product2 > N1,  
6.     !.  
7. is_integer(0).  
8. is_integer(X) :- is_integer(Y), X is Y + 1.
```

- If the condition met, then there is no need to find another number and the cut will terminate the backtracking process.
- Note that the backtracking happen because of **is\_integer** predicate.

## Example 2: Divide two numbers.

- The predicate `is_integer()`. Is responsible for generating an infinite number of integer numbers starting from 0.

```
7. is_integer(0).
```

```
8. is_integer(X) :- is_integer(Y), X is Y + 1.
```

- To understand this, you can ask prolog the following

```
?- is_integer(X) .
```

```
X=0 ;
```

```
X=1 ;
```

```
X=2 ;
```

```
...
```



# Problems with the Cut

- Consider the following adapted version of the append.

```
append([], X, X) :- !.  
append([A|B], C, [A|D]) :- append(B, C, D).
```

- Now, if we ask the following:

```
try append(X, Y, [a,b,c]).
```

- Normally, it should have many solutions. However, the cut operation ‘!’ will terminate the backtracking after the first solution.